| Q. NO. | [ANS] |
| :---: | :---: |
| 1 | A |
| 2 | D |
| 3 | A |
| 4 | C |
| 5 | B |
| 6 | D |
| 7 | A |
| 8 | B |
| 9 | C |
| 10 | A |
| 11 | D |
| 12 | B |
| 13 | A |
| 14 | A |
| 15 | D |
| 16 | C |
| 17 | BONUS |
| 18 | B |
| 19 | A |
| 20 | C |
| 21 | D |
| 22 | B |
| 23 | B |
| 24 | C |
| 25 | C |
| 26 | B |
| 27 | D |
| 28 | A |
| 29 | B |
| 30 | C |
| 31 | C |
| 32 | D |
| 33 | B |
| 34 | A |
| 35 | B |
| 36 | B |
| 37 | C |
| 38 | B |
| 39 | A |
| 40 | B |
| 41 | B |
| 42 | B |
| 43 | B |
| 44 | C |
| 45 | B |

## Single Correct Answer Type

## 1 (a)

$v=\sqrt{2 g R} \therefore \frac{v_{1}}{v_{2}}=\sqrt{\frac{g_{1}}{g_{2}} \times \frac{R_{1}}{R_{2}}}=\sqrt{g \times K}=(K g)^{1 / 2}$
2 (d)
Gravitational potential energy is given as

$$
\begin{aligned}
U & =-\frac{G M m}{r} \\
U_{1} & =-\frac{G M m}{r_{1}}, U_{2}=-\frac{G M m}{r_{2}}
\end{aligned}
$$

As $r_{2}>r_{1}$, hence,
$U_{1}-U_{2}=G M m\left[\frac{r_{2}-r_{1}}{r_{1} r_{2}}\right]$ is positie
ie,

$$
\begin{aligned}
& U_{1}>U_{2} \\
& U_{2}<U_{1}
\end{aligned}
$$

$i e$, gravitational potential energy increases.
3
(a)
$g=\frac{4}{3} \pi G \rho R \Rightarrow g \propto \rho R \Rightarrow \frac{g_{e}}{g_{m}}=\frac{\rho_{e}}{\rho_{m}} \times \frac{R_{e}}{R_{m}}$
$\Rightarrow \frac{6}{1}=\frac{5}{3} \times \frac{R_{e}}{R_{m}} \Rightarrow R_{m}=\frac{5}{18} R_{e}$
4
(c)
$H=\frac{u^{2}}{2 g} \Rightarrow H \propto \frac{1}{g} \Rightarrow \frac{H_{B}}{H_{A}}=\frac{g_{A}}{g_{B}}$
Now $g_{B}=\frac{g_{A}}{12}$ as $g \propto \rho R$
$\therefore \frac{H_{B}}{H_{A}}=\frac{g_{A}}{g_{B}}=12$
$\Rightarrow H_{B}=12 \times H_{A}=12 \times 1.5=18 \mathrm{~m}$

## $5 \quad$ (b)

Gravitational force provides the required centripetal force $i e$,
$m \omega^{2} R=\frac{G M m}{R^{\frac{5}{2}}}$
$\Rightarrow \quad \frac{m 4 \pi^{2}}{T^{2}}=\frac{G M m}{R^{\frac{7}{2}}}$
$\Rightarrow \quad T^{2} \propto R^{7 / 2}$
$6 \quad$ (d)
$v_{0}=\sqrt{\frac{G M}{r}}=\sqrt{\frac{g R^{2}}{R+h}}$
7
(a)

8 (b)
$\frac{T^{2}}{r^{3}}=$ constant $\Rightarrow T^{2} r^{-3}=\mathrm{constant}$
9
(c)
$\frac{T_{\text {mercury }}}{T_{\text {earth }}}=\left(\frac{r_{\text {mercury }}}{r_{\text {earth }}}\right)^{3 / 2}=\left(\frac{6 \times 10^{10}}{1.5 \times 10^{11}}\right)^{3 / 2}=\frac{1}{4}$
(approx.)
$\therefore T_{\text {mercury }}=\frac{1}{4}$ year
10 (a)
As in case of elliptic orbit of a satellite mechanical energy
$E=-(G M m / 2 a)$ remains constant, at any position of satellite in the orbit,
$\mathrm{KE}+\mathrm{PE}=-\frac{G M m}{2 a}$
Now, if at position $r, v$ is the orbital speed of satellite
$\mathrm{KE}=\frac{1}{2} m v^{2}$ and $\mathrm{PE}=-\frac{G M m}{r}$
So, from Eqs. (i) and (ii), we have
$\frac{1}{2} m v^{2}-\frac{G M m}{r}=-\frac{G M m}{2 a}, i e, v^{2}=G M\left[\frac{2}{r}-\frac{1}{a}\right]$
11
(d)
$\frac{K_{A}}{K_{B}}=\frac{r_{B}}{r_{A}}=\left(\frac{R+h_{B}}{R+h_{A}}\right)=\left(\frac{R+2 R}{R+R}\right)=\frac{3}{2}$
12 (b)
From Kepler's third law of planetary motion

$$
T^{2} \propto R^{3}
$$

Given, $T_{1}=1, T_{2}=8, R_{1}=R$
$\therefore \quad \frac{T_{1}^{2}}{T_{2}^{2}}=\frac{R_{1}^{3}}{R_{2}^{3}}$

$$
R_{2}^{3}=R_{1}^{3} \frac{T_{2}^{2}}{T_{1}^{2}}
$$

$$
R_{2}^{3}=R_{1}^{3} \times(8)^{2}
$$

$$
R_{2}^{3}=R^{3} \times\left(2^{3}\right)^{2}
$$

$\Rightarrow \quad R_{2}=R \times 4=4 R$
13 (a)
$g^{\prime}=\frac{G M}{(R+h)^{2}}$, acceleration due to gravity at height $h$
$\Rightarrow \quad \frac{g}{9}=\frac{G M}{R^{2}} \cdot \frac{R^{2}}{(R+h)^{2}}$

$$
=g\left(\frac{R}{R+h}\right)^{2}
$$

$\Rightarrow \quad \frac{1}{9}=\left(\frac{R}{R+h}\right)^{2}$
$\Rightarrow \frac{R}{R+h}=\frac{1}{3}$
$\Rightarrow \quad 3 R=R+h$
$\Rightarrow \quad 2 R=h$
14 (a)
Since the gravitational field is conservative field, hence, the work done in taking a particle from one point to another in a gravitational field is path independent
15
(d)

At height $h^{\prime}, \frac{\mathrm{g}}{\mathrm{g}}=1-\frac{2 h}{R}=\frac{90}{100}$
or $\frac{2 h}{R}=1-\frac{90}{100}=\frac{10}{100}=\frac{1}{10}$
or $R=20 \mathrm{~h}=20 \times 320=6400 \mathrm{~km}$
At dept $d, \frac{\mathrm{~g}^{\prime}}{\mathrm{g}}=1-\frac{d}{R}=\frac{95}{100}$
or $\frac{d}{R}=1-\frac{95}{100}=\frac{5}{100}=\frac{1}{20}$
or $d=\frac{R}{20}=\frac{6400}{20}=320 \mathrm{~km}$
(c)
$T=2 \pi \sqrt{\frac{r^{3}}{G M}} \Rightarrow T^{2}=\frac{4 \pi^{2}}{G M}(R+h)^{3}$
$\Rightarrow R+h=\left[\frac{G M T^{2}}{4 \pi^{2}}\right]^{1 / 3} \Rightarrow h=\left[\frac{G M T^{2}}{4 \pi^{2}}\right]^{\frac{1}{3}}-R$
17 (bonus)
From Kepler's third law of planetary motion also known as law of periods

18 (b)
$v_{e}=\sqrt{2} v_{0}$, i.e. if the orbital velocity of moon is increased by factor of $\sqrt{2}$ then it will escape out from the gravitational field of earth
$20 \quad$ (c)
Force on the body $=\frac{G M m}{x^{2}}$
To move it by a small distance $d x$,
Work done $=F d x=\frac{G M m}{x^{2}} d x$
Total work done $=G M m \int_{R}^{R+h} \frac{d x}{x^{2}}=\left[\frac{-G M m}{x}\right]_{R}^{R+h}$
$=G M m\left[\frac{1}{R}-\frac{1}{R+h}\right]$
$=\left[\frac{(R+h)-R}{R(R+h)}\right]=\frac{G M m h}{R(R+h)}$
$\frac{G M}{R^{3}} \times \frac{m h R}{R+h}=\frac{g m h R}{R+h}=\frac{P R h}{R+h}$
21
(d)
$T=2 \pi \sqrt{\frac{l}{g}} \Rightarrow T \propto \frac{1}{\sqrt{g}} \Rightarrow \frac{T_{P}}{T_{e}}=\sqrt{\frac{g_{e}}{g_{P}}}=\sqrt{\frac{2}{1}} \Rightarrow T_{P}=\sqrt{2} T_{e}$
22 (b)
$\frac{d^{2} x}{d t^{2}}=-\alpha x$
We know,

$$
a=\frac{d^{2} y}{d t^{2}}=-\omega^{2} x
$$

From Eqs.(i) and (ii), we have

|  | $\omega^{2}=\alpha$ |
| :--- | ---: |
|  | $=$$\alpha$ <br> or <br> $\therefore$ |
|  | $\frac{2 \pi}{T}=\sqrt{\alpha}$ |
|  | $T=\frac{2 \pi}{\sqrt{\alpha}}$ |

23 (b)
Motion given here is SHM starting from rest
$24 \quad$ (c)
The average acceleration of a particle performing SHM over one complete oscillation is zero.
26 (b)
$x=A \cos (\omega t+\theta)$;
Velocity, $v=\frac{d x}{d t}=-A \omega \sin (\omega t+\theta)$
$=-A \omega \sqrt{1-\cos ^{2}(\omega t+\theta)}$
$=-A \omega \sqrt{1-x^{2} / A^{2}}=-\omega \sqrt{A^{2}-x^{2}}$
Here, $v=\pi \mathrm{cms}^{-1}, x=1 \mathrm{~cm}, \omega=\pi \mathrm{s}^{-1}$
So $\pi=-\pi \sqrt{A^{2}-1^{2}}$
or $(-1)^{2}=A^{2}-1$ or $A^{2}=2$
or $A=\sqrt{2} \mathrm{~cm}$
27 (d)
For simple harmonic motion, $y=a \sin \omega t$

$$
\begin{align*}
\therefore \quad y=a \sin & \left(\frac{2 \pi}{T}\right) t \\
y_{1} & =a \sin \left[\left(\frac{2 \pi}{16}\right) \times 2\right] \\
& =a \sin \left(\frac{\pi}{4}\right)=\frac{a}{\sqrt{2}} \tag{i}
\end{align*}
$$

At $t=4 \mathrm{~s}$ or after 2 s from mean position.

$$
y_{1}=\frac{a}{\sqrt{2}}, \text { velocity }=4 \mathrm{~ms}^{-1}
$$

$\therefore$ Velocity $=\omega \sqrt{a^{2}-y_{1}^{2}}$
or $\quad 4=\left(\frac{2 \pi}{16}\right) \sqrt{a^{2}-\frac{a^{2}}{2}}$
[From Eq. (i)]
or $\quad 4=\frac{\pi}{8} \times \frac{a}{\sqrt{2}}$
or $\quad a=\frac{32 \sqrt{2}}{\pi} \mathrm{~m}$
28 (a)
The given equation is written as,

$$
\begin{equation*}
y=3 \sin \left(100 t+\frac{\pi}{6}\right) \tag{i}
\end{equation*}
$$

The general equation of simple harmonic motion is written as

$$
\begin{equation*}
y=a \sin (\omega t+\emptyset) \tag{ii}
\end{equation*}
$$

Equating Eqs. (i) and (ii), we get

$$
a=3, \omega=100
$$

Maximum velocity, $v=a \omega$

$$
=3 \times 100=300 \mathrm{~ms}^{-1}
$$

29 (b)
Length of the line = Distance between extreme positions of oscillation $=4 \mathrm{~cm}$
So, Amplitude $a=2 \mathrm{~cm}$
also $v_{\text {max }}=12 \mathrm{~cm} / \mathrm{s}$
$\because v_{\max }=\omega a=\frac{2 \pi}{T} a$
$\Rightarrow T=\frac{2 \pi a}{v_{\max }}=\frac{2 \times 3.14 \times 2}{12}=1.047 \mathrm{~s}$
30
(c)

When $t=\frac{T}{12}$, then $x=A \sin \frac{2 \pi}{T} \times \frac{T}{12}=\frac{A}{2}$

$$
\begin{aligned}
\mathrm{KE} & =\frac{1}{2} m v^{2}=\frac{1}{2} m \omega^{2}\left(r^{2}-x^{2}\right) \\
& =\frac{1}{2} m \omega^{2}\left(A^{2}-\frac{A^{2}}{4}\right) \\
& =\frac{3}{4}\left(\frac{1}{2} m \omega^{2} A^{2}\right) \\
\mathrm{PE} & =\frac{1}{2} m \omega^{2} x^{2}=\frac{1}{4}\left(\frac{1}{2} m \omega^{2} A^{2}\right) \\
\frac{\mathrm{KE}}{\mathrm{PE}} & =\frac{3}{1}
\end{aligned}
$$

31
(c)

The bob possess kinetic energy at its mean position which gets converted to potential energy at height $h$. But the total energy remains converted.


Hence, we have

## $\mathrm{KE}=\mathrm{PE}$

Let velocity of the bob at mean position be $v$ and $m$ be its mass, then we have

$$
\begin{array}{ll} 
& \frac{1}{2} m v^{2}=m g h \\
\Rightarrow & v=\sqrt{2 g h} \\
& \text { Putting } g=9.8 \mathrm{~ms}^{-2}, h=0.1 \mathrm{~m} \\
\therefore & v=\sqrt{2 \times 9.8 \times 0.1}=1.4 \mathrm{~ms}^{-1}
\end{array}
$$

32 (d)
$y=a \sin \omega t ; v=\frac{d y}{d t}=a \omega \cos \omega t$
$=a \omega \sin (\omega t+\pi / 2)$
Acceleration $A=\frac{d v}{d t}=-\omega^{2} a \sin \omega t$
$=\omega^{2} a \sin (\omega t+\pi)$
33
(b)

Maximum acceleration $=$ Maximum velocity $\times \pi$
ie, $\quad \omega^{2} A=\pi \omega A$
where $A$ is amplitude and $\omega$ is angular velocity.
$\Rightarrow$
$\omega=\pi$
$\Rightarrow \quad \frac{2 \pi}{T}=\pi$
$\Rightarrow \quad T=2 \mathrm{~s}$
34
(a)

At the time $t=\frac{T}{4}=\frac{4}{4}=1 \mathrm{sec}$ after passing from mean position, the body reaches at it's extreme position. At extreme, position velocity of body becomes zero
35 (b)
$y=4 \cos ^{2}\left(\frac{t}{2}\right) \sin 1000 t$
$\Rightarrow y=2(1+\cos t) \sin 1000 t$
$\Rightarrow y=2 \sin 1000 t+2 \cos t \sin 1000 t$
$\Rightarrow y=2 \sin 1000 t+\sin 999 t+\sin 1001 t$
It is a sum of three S.H.M.
36 (b)
PE varies from zero to maximum. It is always positive sinusoidal function
37 (c)
$y=A \sin P T+B \cos P T$
Let $A=r \cos \theta, B=r \sin \theta$
$\Rightarrow y=r \sin (P T+\theta)$ which is the equation of SHM
38
(b)
$n=\frac{1}{2 \pi} \sqrt{\frac{g}{l}} \Rightarrow n \propto \frac{1}{\sqrt{l}} \Rightarrow \frac{n_{1}}{n_{2}}=\sqrt{\frac{l_{2}}{l_{1}}}=\sqrt{\frac{L_{2}}{2 L_{2}}}$
$\Rightarrow \frac{n_{1}}{n_{2}}=\frac{1}{\sqrt{2}} \Rightarrow n_{2}=\sqrt{2} n_{1} \Rightarrow n_{2}>n_{1}$
Energy $E=\frac{1}{2} m \omega^{2} a^{2}=2 \pi^{2} m n^{2} a^{2}$
$\Rightarrow \frac{a_{1}^{2}}{a_{2}^{2}}=\frac{m_{2} n_{2}^{2}}{m_{1} n_{1}^{2}} \quad[\because E$ is same $]$
Given $n_{2}>n_{1}$ and $m_{1}=m_{2} \Rightarrow a_{1}>a_{2}$
$39 \quad$ (a)
On the inclined plane, the effective acceleration due to gravity
$\mathrm{g}^{\prime}=\mathrm{g} \cos 30^{\circ}$
$=g \times \sqrt{3} / 2$
$\therefore \quad \mathrm{T}=2 \pi \sqrt{\frac{1}{\mathrm{~g}^{\prime}}}=2 \pi \sqrt{\frac{2 \mathrm{l}}{\sqrt{3} g}}$
$40 \quad$ (b)


So $B=A, \phi=240^{\circ}=\frac{4 \pi}{3}$

## Assertion - Reasoning Type

42 (b)
Acceleration due to gravity,
$g^{\prime}=g-R \omega^{2} \cos ^{2} \lambda$
At equator, $\lambda=0^{\circ}$ i.e. $\cos 0^{\circ}=1 \therefore g_{e}=g-R \omega^{2}$
At poles, $\lambda=90^{\circ}$ i.e. $\cos 90^{\circ}=0 \therefore g_{p}=g$
Thus, $g_{p}=g_{e}=g-g+R \omega^{2}=R \omega^{2}$
Also, the value of $g$ is maximum at poles and minimum at equators

## 43 (b)

If root mean square velocity of the gas molecules is less than escape velocity from that planet (or satellite) then atmosphere will remain attached with that planet and if $v_{r m s}>u_{\text {escape }}$ then there will be no atmosphere on the planet. This is the reason for no atmosphere at moon

## $44 \quad$ (c)

Amplitude of oscillation for a forced, damped oscillator is $A=\frac{F_{0} / m}{\sqrt{\left(\omega^{2}-\omega_{0}^{2}\right)+(b \omega / m)^{2}}}$, where $b$ is constant related to the strength of the resistive force, $\omega_{0}=\sqrt{k / m}$ is natural frequency of undamped oscillator ( $b=0$ )

When the frequency of driving force $(\omega) \approx \omega_{0}$, then amplitude $A$ is very larger.

For $\omega<\omega_{0}$ or $\omega>\omega_{0}$, the amplitude decreases
45
(b)

In simple pendulum, when bob is in deflection position, the tension in the spring is $T=m g \cos \theta+\frac{m v^{2}}{l}$. Since the value of $\theta$ is different at different positions, hence tension in the string is not constant throughout the oscillation


At end points $\theta$ is maximum; the value of $\cos \theta$ is least, hence the value of tension in the string is least. At the mean position, the value of $\theta=0^{\circ}$ and $\cos 0^{\circ}=1$, so the value of tension is largest

Also velocity is given by $v=\omega \sqrt{a^{2}-y^{2}}$ which is maximum when $y=0$, at mean position

